Challenge 317: Is u an integer?

Suppose that $x^2 + x + 1 = u^2$, where x is an integer.

Show that $(2u)^2 - 3$ must be a perfect square, and hence find all the values of x for which u is also an integer.