Challenge 363: Strangely Simultaneous

Given that $4x^2 + 2xy + y^2 = 111$ and xy = 18, how many x-values satisfy both equations? What is the sum of the squares of these x-values?

Use algebra to answer these questions, but make it as simple as you can!